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ЦЕНТРАЛЬНЫЙ НАУЧНО-ИССЛЕДОВАТЕЛЬСКИЙ ИНСТИТУТ
ИНФОРМАЦИИ И ТЕХНИКО-ЭКОНОМИЧЕСКИХ ИССЛЕДОВАНИЙ
ПО АТОМНОЙ НАУКЕ И ТЕХНИКЕ

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ELECTRON SCATTERING FROM LIGHT NUCLEI
IN THE REGIONS OF QUASI-ELASTIC PEAK
AND Δ -ISOBAR EXCITATION

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The cross sections of the (e, e') reaction on nuclei are considered in the identical form for the quasi-elastic electron scattering and the quasi-free pion electroproduction. The cross sections on single nucleon in the Δ -isobar excitation region are obtained using the dispersion relations being in good agreement with the experiment. A consistent set of parameters for the shell model with the oscillator potentials is obtained for ^{12}C , ^{16}O , ^{20}Ne , ^{24}Mg , ^{28}Si nuclei. The mean square radii of the nuclei charge distribution calculated with the use of these parameters agree with the rms obtained from the electron-nuclei elastic scattering experiments.

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РАССЕЯНИЕ ЭЛЕКТРОНОВ НА ЛЕГКИХ ЯДРАХ
В ОБЛАСТИ РОЖДЕНИЯ Δ - ИЗОБАРЫ И КВАЗИУПРУГОГО
ПИКА

В предположении квазисвободных нуклонов строятся сечения процесса (e, e') на ядрах в едином виде для областей квазиупругого пика и Δ - изобары. Сечения на отдельных нуклонах в области рождения Δ - изобары получены с помощью дискретизированных соотношений и хорошо согласуются с экспериментом. Для ядер Be , C , Mg , Al , Si получен согласованный набор параметров для оболочечной модели с осцилляторными потенциалами. Среднеквадратичные радиусы распределения заряда ядер, вычисленные с этими параметрами, согласуются с величинами радиусов, полученными из экспериментов по упругому рассеянию электронов на ядрах.

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Introduction

At present, there are experiments [1,2] on electron-nuclei scattering, in which measurements were performed for a set of nuclei in the quasi-elastic peak as well as in inelastic region. Analyzing these data in the Δ -isobar region using the dispersion relations we have concluded that the cross sections on nuclei in this energy region are very sensitive to the nuclear models. This fact is connected with the pion production total cross section high sensitivity arising when taking into account Fermi motion and also with resonance nature of the processes on single nucleon. Therefore a joint analysis of the data in both regions (quasi-elastic scattering and pion electroproduction) enables one to obtain a more confident information on investigated models of a nucleus.

The shell models with different form of potentials are widely used in the analysis of experimental results on the light nuclei. Among them the model with oscillator potential is a most popular one. The $(e, e'p)$, $(p, 2p)$ experiments confirmed reliably the shell structure of nuclei and showed that the protons on different shells move at different potentials. At present, the information on binding energies E for protons on different shells is available [3,4,5] for many nuclei with $A < 40$ with an

accuracy from one up to several MeV. As to the parameters of the oscillator model p_0 which are responsible for the momentum distribution of nucleons in nucleus, they are determined from the experiment indirectly, and there is no agreement in their values obtained in various investigations. For example, the oscillator parameters for carbon [3] are 1.5-2 times as high as those for ${}^6\text{Li}$ and ${}^9\text{Be}$ [5], being at the same time higher than for ${}^{28}\text{Si}$ [6]. For the other nuclei, there is practically no satisfactory information on the oscillator parameters for different shells. One of the aims of this paper is to test the possibility of consistent description of a set of light nuclei using the oscillator shell model assuming that nuclei having close atomic numbers would differ from each other due mainly to the outer unfilled shells.

This paper contains three sections.

In Sect. 1 we deal mainly with obtaining the cross section in the Δ isobar region on a free nucleon using the dispersion relations over invariant mass of produced hadrons S . A good agreement with the experimental data on protons and deuterons is obtained.

In Sect. 2 the electron-nucleus cross sections are constructed, assuming impulse approximation in the identical form both for the elastic and resonance regions. A form of the cross sections is suggested, which permits us to spread to the resonance region the ideas of the shell model usually intended as a description of quasi-elastic peak. A similar approach was originally used by Atwood and West [7] for the deep-inelastic electron-nucleon scattering region.

In Sect. 3 the results of calculations for ${}^{12}\text{C}$, ${}^{16}\text{O}$, ${}^{20}\text{Ne}$, ${}^{24}\text{Mg}$ and ${}^{28}\text{Si}$ are presented. It is shown that the initial assumptions concerning the shell model and the way of its application to the region of Δ resonance are in good agreement with the experimental data.

1. Electron Scattering on Free Nucleon in Elastic
and Resonance Regions

Assuming one-photon exchange approximation the cross section of electron-nucleon elastic scattering as well as the total cross section of pion electroproduction in the resonance region are convenient to express in the identical form, in which the contributions of transversely and longitudinally polarized photons are separated explicitly:

$$\frac{d^2\sigma^{e\ell}}{dE_2 d\Omega} = \frac{4\alpha^2 M}{\lambda^2} \frac{E_2}{E_1} \frac{1}{1-\varepsilon} (\tau G_M^2(\lambda^2) + \varepsilon G_E^2(\lambda^2)) \delta(s-M^2), \quad (1)$$

$$\frac{d^2\sigma^A}{dE_2 d\Omega} = \Gamma (\sigma_T(s, \lambda^2) + \varepsilon \sigma_L(s, \lambda^2)) \theta(s - (M + \mu)^2), \quad (2)$$

$$\lambda^2 = -q^2 = 2E_1 E_2 (1 - \cos\theta), \quad \tau = \lambda^2 / 4M^2, \quad (3)$$

$$\varepsilon = \left(1 + 2 \frac{|\vec{q}_1|}{\lambda^2} \tan^2 \frac{\theta}{2}\right)^{-1}, \quad \Gamma = \frac{\alpha}{2\pi^2 \lambda^2} \frac{s-M^2}{2M} \frac{1}{1-\varepsilon} \frac{E_2}{E_1}, \quad (4)$$

$$s = (q + p)^2 = M^2 + 2Mq_0 - \lambda^2. \quad (5)$$

Here M and μ are masses of nucleon and pion, $p(p_0, \vec{p})$ and $q(q_0, \vec{q})$ are four-momenta of nucleon and photon, respectively, E_1 and E_2 are the energies of the incident and outgoing electrons in the lab. system, θ is the angle between directions of these electrons.

In expression (1) for the electron-nucleon elastic scattering $G_M(\lambda^2)$ and $G_E(\lambda^2)$ are the Sachs nucleon formfactors which at $\lambda^2 \ll 1 \left(\frac{\text{GeV}}{c}\right)^2$ are described well by the dipole formula

$$G \sim (1 + \lambda^2/0,71)^{-2}$$

To calculate the electroproduction cross section we use the dispersion relations for the invariant amplitudes $A_1(s,t) \dots A_6(s,t)$ [8] at a fixed momentum transfer t . Note the main points of our calculations.

The real part of the amplitudes consists of the contributions of the Born diagrams (which include the formfactors of nucleons and pions) and the dispersion integrals from the imaginary parts of the corresponding amplitudes. The pion formfactor in the considered region is described well by VDM and has the form $F_\pi(\lambda^2) = (1 + \lambda^2/0,5)^{-1}$.

An essential difference of pion electroproduction from the real photoproduction in the resonance region consists in appearance of λ^2 -dependence of the resonance couplings γ_{NN^*} as well as in appearance of longitudinal amplitudes. In Ref. [9] using the dispersion relations the analysis of available by that time experimental data on proton was carried out. In this analysis a λ^2 -parametrization of multipole amplitudes with relatively small number of fit parameters was suggested proceeding from analyticity and definite asymptotical behaviour of total cross sections at large λ^2 . In calculations we used the results obtained in this analysis for multipoles M_{1+} , E_{1+} and S_{1+} , corresponding to resonance F_{15} (1230).

The dispersion integrals are determined mainly by the F_{15} (1230) resonance contribution. To estimate the high-energy contributions we included in the consideration also the contributions of resonances with larger masses F_{13} (1440), F_{13} (1680) and F_{15} (1680) which, as shown in the analysis [9], pronounced distinctly in pion electroproduction. Their contribution turned out to be negligible in the first resonance region.

To eliminate the kinematic singularities in invariant amplitudes

$A_2(s,t)$ and $A_5(s,t)$ a subtraction procedure is usually used [8]. The calculations showed that the subtraction contribution in the cross section is negligible.

Thus the below-given results in the first resonance region practically were obtained with the help of the amplitudes whose imaginary parts are determined by the P_{33} (1232) resonance, while the real parts consist of the contributions of the Born diagrams and dispersion integrals where only the P_{33} (1232) resonance contribution is taken into account.

Fig. 2 presents the results of our calculations for electroproduction in the region of the P_{33} (1232) resonance on proton. One can see that there is a good agreement with the experiment [2,10].

To check up the results of calculations on neutron we calculated the cross sections on deuteron with the wave functions taken according to Ref.[11]. As is seen from Fig. 2, the agreement with the experiment is good.

2. Electron Scattering on Nuclei

Let us assume for a moment that a nucleus is a set of free moving nucleons and the probability of scattering on a nucleus is added from the probabilities of the processes on free nucleons; hence the electron-nucleus cross section can be written as

$$d\sigma^A = \frac{1}{I^A} \sum^A \int d\sigma^N(s,p,\lambda^2) I^N \rho(\vec{p}) d\vec{p}, \quad (7)$$

where I^A , I^N are invariant fluxes on nucleus and nucleon, respectively, $\rho(\vec{p})$ is the density of nucleon momentum distribution.

In order to obtain expressions for the cross section on moving nucleon we make in invariant cross sections (1, 2) the Lorentz transformation into

the system moving with a velocity \vec{p}/p_0 . Omitting the intermediate formulae present a final form of the cross section for electron scattering on moving nucleon:

$$\frac{d^2\sigma}{dE_2' d\Omega'} = \Gamma^{-1} (\sigma_T(s, p, \lambda^2) + \varepsilon \sigma_L(s, p, \lambda^2) + \sqrt{2\varepsilon(1-\varepsilon)} \sigma_{LT}(s, p, \lambda^2)), \quad (8)$$

$$\sigma_T(s, p, \lambda^2) = \sigma_T(s, \lambda^2) + \frac{\lambda^2 p^2 \sin^2 \theta_p}{2M^2 |q'|^2} (\sigma_T(s, \lambda^2) + \sigma_L(s, \lambda^2)), \quad (9)$$

$$\sigma_L(s, p, \lambda^2) = \sigma_L(s, \lambda^2) + \frac{\lambda^2 p^2 \sin^2 \theta_p}{|q'|^2 M^2} (\sigma_T(s, \lambda^2) + \sigma_L(s, \lambda^2)) (\cos^2 \varphi + \frac{1}{2}), \quad (10)$$

$$\sigma_{LT}(s, p, \lambda^2) = (\sigma_T(s, \lambda^2) + \sigma_L(s, \lambda^2)) (q_0 |\vec{p}| \cos \theta_p - p_0 |\vec{q}'|) \frac{|p| \lambda^2 (E_1 + E_2)}{|q'|^2 |\vec{q}'|^2} \sin \theta_p \cos \varphi, \quad (11)$$

$$s = (p+q)^2 = M^2 - \lambda^2 + 2p_0 q_0 - 2|p||q| \cos \theta_p, \quad |q'|^2 = \frac{(s - M^2 + \lambda^2)^2}{4M^2} + \lambda^2. \quad (12)$$

Here θ_p and φ are polar and azimuthal angles of nucleon momentum if the Z axis coincides with a direction of q-momentum of virtual proton. The kinematic variables in the rest system of the target nucleon are characterized by a prime.

Substitute now the expression (8) into formula (7) taking into account that in the rest system of target nucleus $I^A = E_1 M_q$, $I^N = E_1' M = \sqrt{E_1 p_0 - K_1 p}$ and from the invariance of the four-dimensional phase volume there follows $dE_2' d\Omega' = dE_2 d\Omega E_2 / E_2'$. Performing simultaneously the integration over azimuthal angle φ we arrive at the following expression for the cross section of the production of nucleus

$$\frac{d^2\sigma^A}{dE_2 d\Omega} = \frac{\alpha}{2\pi} \frac{E_2}{E_1} \frac{\lambda^2}{1-\varepsilon} (\sigma_T^A(\lambda^2) + \varepsilon \sigma_L^A(\lambda^2)), \quad (13)$$

$$\tilde{\sigma}_{T,L}^A(\lambda^2) = 2\pi \int p(\bar{p}) \frac{s-M^2}{2M} \sigma_{T,L}^N(s, p, \lambda^2) \theta(s-(M+\mu)^2) \bar{p}^2 d|\bar{p}| d\cos\theta_p. \quad (14)$$

The cross sections on single nucleon $\sigma_{T,L}^N(s, p, \lambda^2)$ are given by formulae (9-10) with the obvious simplification $(\cos^2\varphi + \frac{1}{2}) \rightarrow 1$ for σ_L^N because of the integration over φ .

The cross section of knocking out of the free nucleon from the nucleus is obtained from (13-14) and (9-10) by the replacements

$$\frac{\alpha \lambda^2}{2\pi} \rightarrow \frac{4Md^2}{\lambda^2}, \quad \frac{s-M^2}{2M} \rightarrow 1, \quad \theta(s-(M+\mu)^2) \rightarrow \delta(s-M^2), \quad (15)$$

$$\sigma_T^N(s, \lambda^2) \rightarrow \tau G_M^2(\lambda^2), \quad \sigma_L^N(s, \lambda^2) \rightarrow G_E^2(\lambda^2).$$

When turning to electron scattering on real nuclei, there arises a question on validity of application of formulae (13,14) corresponding to quasi-free picture of nucleons. In the region under consideration, $\lambda^2 \geq 0,2 \left(\frac{\text{GeV}}{c}\right)^2$, the contributions of the coherent processes are small, and the effects connected with re-scattering of final particles as well as with the account of the Pauli principle may apparently be neglected.

To take into account the Fermi momentum of the target nucleons we have used the cross sections (7-10) for a free moving nucleon, where for nucleon on mass-shell the squared invariant mass of final hadrons was defined by formula (12). For the bound nucleon ($p_0^2 \neq \bar{p}^2 + M^2$) from the diagram corresponding to the impulse approximation (Fig.1) the invariant mass of final hadrons may be estimated not assuming relations between energy and

momentum of intermediate nucleon. We proceed from the following definition:

$$\begin{aligned}
 s &= p_x^2 = (p_A - p_{A-1} + q)^2 = \\
 &= s_0 - 2(q_0 + M)(\epsilon + T_{A-1}) - \bar{p}^2 - 2|\bar{p}||\bar{q}|\cos \theta_p, \quad (16)
 \end{aligned}$$

$$s_0 = M^2 + 2q_0 M - \lambda^2,$$

applicable to any nucleus if under ϵ the binding energy of nucleon on the given shell for the given nucleus is implied. Here T_{A-1} is kinetic energy of the residual nucleus, $\bar{p}_{A-1} = -\bar{p}$, the other designations are defined according to Fig. 1. For the calculations with use of the Fermi model ϵ would denote mean energy of separation of nucleon from nucleus.

Although we ignore partially the off-shell effects for the bound nucleon assuming in $\tilde{\sigma}_{TL}^N(s, p, \lambda^2)$ the λ^2 dependence being the same as the one for the free nucleon, nevertheless, having defined $\tilde{\sigma}_{TL}^N(s, p, \lambda^2)$ in (13), we have accounted these effects through the main variables s and λ^2 for the strong energy structure (resonance or S -functions) in the total cross sections in the considered region $\sqrt{s} \leq 1.5$ GeV.

For comparison we introduced into (16) the quantity $\epsilon_0 = \epsilon + T_{A-1}$ (average kinetic mass of final hadrons produced on a free nucleon or meson), which has been used as a variable for energy spectra on nuclei. In a similar way we define ϵ_0 for the meson side (the nuclei ϵ and T_{A-1} are defined correspondingly).

For the meson side we consider the production of nucleon-antinucleon pairs $N\bar{N}$ and $\Lambda\bar{\Lambda}$ pairs. For the nucleon side we consider the production of $\Lambda\bar{\Lambda}$ pairs and $N\bar{N}$ pairs. For the meson side we consider the production of $\Lambda\bar{\Lambda}$ pairs and $N\bar{N}$ pairs.

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knocked-out nucleon is dominant, from (16) for the energy of the ejected nucleon $E_{\bar{p}+\bar{q}}$ follows the expression

$$E_{\bar{p}+\bar{q}} = M + q_0 - \epsilon - T_{A-1},$$

usually used in investigation of the $(e, e'p)$ reaction. The use of variable S is preferable because it allows us to include promptly the inelastic processes. Thus the cross section on nucleus is determined by integrals (14) over phase volume of moving nucleon with the weighting functions

$$\tilde{\sigma}_{T,L}^N(s, p, \lambda^2) = \tilde{\sigma}_{T,L}^A(s, p, \lambda^2) \theta(S - (M+M)^2) + \tilde{\sigma}_{T,L}^{\bar{e}e}(s, p, \lambda^2) \delta(S - M^2), \quad (17)$$

where $\tilde{\sigma}_{T,L}^A$ and $\tilde{\sigma}_{T,L}^{\bar{e}e}$ are defined in (9, 10, 15).

Expressions (13-17) together with the use of the shell model for determination of nucleon momentum distribution are a generalization of the approach developed in Refs. [7] for deuteron for the case of nuclei with $A > 2$.

Results

We have done numerical calculations for two groups of nuclei with close atomic numbers ${}^6\text{Li}$, ${}^9\text{Be}$, ${}^{12}\text{C}$, and ${}^{24}\text{Mg}$, ${}^{27}\text{Al}$, ${}^{28}\text{Si}$. The nucleon momentum distribution was assumed to correspond to the oscillator shell model with including only 10 shells.

Binding energies ϵ for the light nuclei are known from the $(e, e'p)$ and $(p, 2p)$ experiments with an accuracy from one to several MeV (see, e.g. [3-5]). The values of these parameters used in our calculations and listed in the Table are obtained for reasons of a better description of the experiment and agree with the data of [3-5].

The oscillator parameters ρ_0 characterizing the nucleon momentum distribution in nucleus were chosen also for reasons of a better description of the experiment with certain restrictions. As a starting meaning for these parameters there served the values of ρ_0 for carbon taken from experiment [3]. The parameters for the other nuclei were arranged in accordance with the conclusion [13] about almost linear growth of ρ_0 with increasing the atomic number A for the inner shells, as well as proceeding from the requirement that the parameters of the closed shells of the nuclei with near-by A would not differ too much. After establishment of quantities ρ_0 for the inner shells the values of parameters for outer shells were finally fitted. Various sensitivity of the cross sections in the regions of quasi-elastic and resonance peaks to parameters ρ_0 and ρ_1 was studied to strictly control these quantities. For comparison the experimental cross sections for carbon [5] are given in the Table for parameters ρ_0 and ρ_1 .

Figs. 3-4 present the results of our calculations for the experiment [1] for Li, C, Mg and Be nuclei at $\omega = 20$ and 30 MeV. It is seen that the obtained curves describe well the experimental data and reproduce the main features of scattered electron energy spectra: positions of maxima and the shapes of both quasi-elastic scattering and resonance excitation peaks.

From the results of calculations the dependence of the cross sections on the angle of scattering θ emerges. It has been shown that the cross section σ_{QE} is a decreasing function of the angle θ for the particles $\theta < 90^\circ$ and σ_{QE} is a increasing function of the angle θ for the value of the angle $\theta > 90^\circ$. The resonance excitation cross sections are sensibly only smaller than those given in [5] for particles $\theta < 90^\circ$. The reason of this is that the calculations are done for the particles $\theta < 90^\circ$ and the resonance excitation cross sections are calculated for the particles $\theta > 90^\circ$.

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however to reach an agreement with the experiment they had to introduce the suppression coefficients connected with nucleon absorption [14] inside the nucleus. These coefficients (0.2 ± 0.5 for $(e, e'p)$ and 0.5 ± 0.8 for $(e, p, 2p)$) are large and cannot be calculated precisely; therefore they may include both effects: real absorption and underestimation of parameters

ρ_0 . The magnitude of the so-called mean-square radius of nucleus charge distribution $\langle r^2 \rangle^{1/2}$ is determined by the same parameters ρ_0 . The difficulties concerning the consistency of this quantity derived from different physical processes - the electron elastic scattering on nuclei and the quasi-elastic scattering on bound nucleons inside nucleus are mentioned in our work (see also Ref. 6). The Table lists the values of $\langle r^2 \rangle^{1/2}$ calculated with our parameters in comparison with the quantities obtained from the elastic scattering data. All quantities are in fm. It can be observed for Mo and Sn, nevertheless, the underestimation of oscillator parameters for the whole nuclear group leads to the underestimation of the nuclei mean square radii.

In the section devoted to the quasi-elastic excitation of the experimentally observed peaks, the comparison was made between the theoretical calculations and the experimental data. The calculations were performed with the use of the oscillator model with the parameters determined in the previous section. The results are shown in Fig. 1. It can be seen that the agreement between the theoretical calculations and the experimental data is not very good. It is impossible to remove the discrepancy by changing the oscillator parameters. The only way to improve the agreement is to change the experimental data. It is not clear, however, how to do this. The experimental data for ^{116}Sn and ^{138}Sn are the best. The agreement between the theoretical calculations and the experimental data is not very good. It is impossible to remove the discrepancy by changing the oscillator parameters. The only way to improve the agreement is to change the experimental data. It is not clear, however, how to do this. The experimental data for ^{116}Sn and ^{138}Sn are the best.

ne nucleon inside nucleus are of the same order of magnitude thus enhancing the probability of the correlative processes.

Note in conclusion that we have carried out calculations assuming that the proton and neutron shell parameters are equal. As is mentioned in Ref. 19, investigations of $(e, e'n)$ processes are at the limit of the present-day experiment feasibilities. Therefore the processes (e, e') remain practically the only source to obtain information on neutron shells in the electron experiments. In the quasi-elastic peak region the neutron cross sections are suppressed as compared to the proton ones, especially at small λ^2 , therefore a relative weight of neutron shell contributions is small. In the resonance region total cross sections on neutrons and protons are approximately equal [20], hence the resonance region is more sensitive to the neutron shell parameters. Unfortunately, there aren't at present many nuclei for which there exist experiments covering besides the quasi-elastic peak also the resonance region. Meanwhile, such data for the values of E_1 and λ^2 , at which both peaks are pronounced well, are of undoubted interest also from the viewpoint of studying neutron distribution in nucleus.

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Table

E, MeV	E, MeV/c	d		E, MeV	P ₀ , MeV/c	$\langle r^2 \rangle^{1/2}$, fm	
		This work	Flastic scattering [15]			This work	Flastic scattering [15]
4	110	-	-	-	-	2.2	-
15	120	-	-	-	-	2.21	2.19
15 (16)	120 (120)	-	-	-	-	2.27 (2.85±25)	2.37
90	120	120	120	120	120	2.6	3.12
90	90	90	90	90	90	3.06	3.06
90	112	112	112	112	112	2.7	3.12

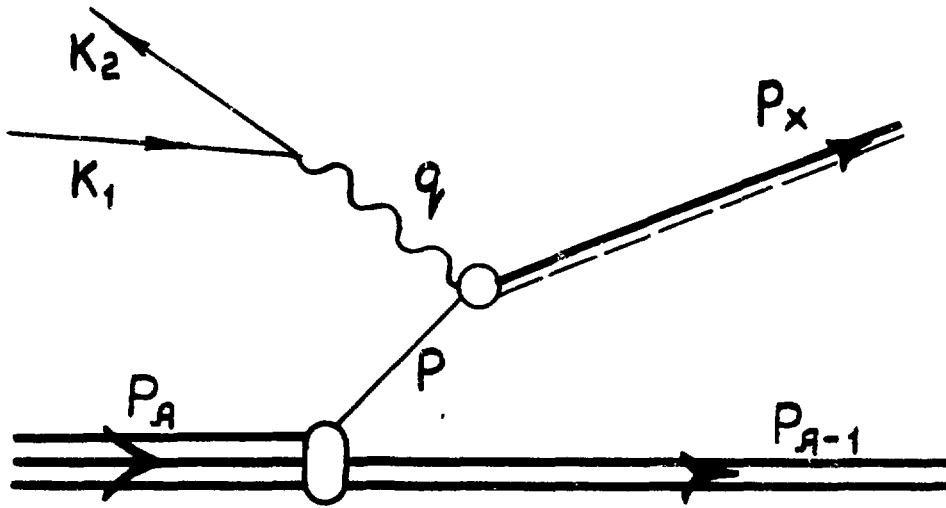


Fig.1

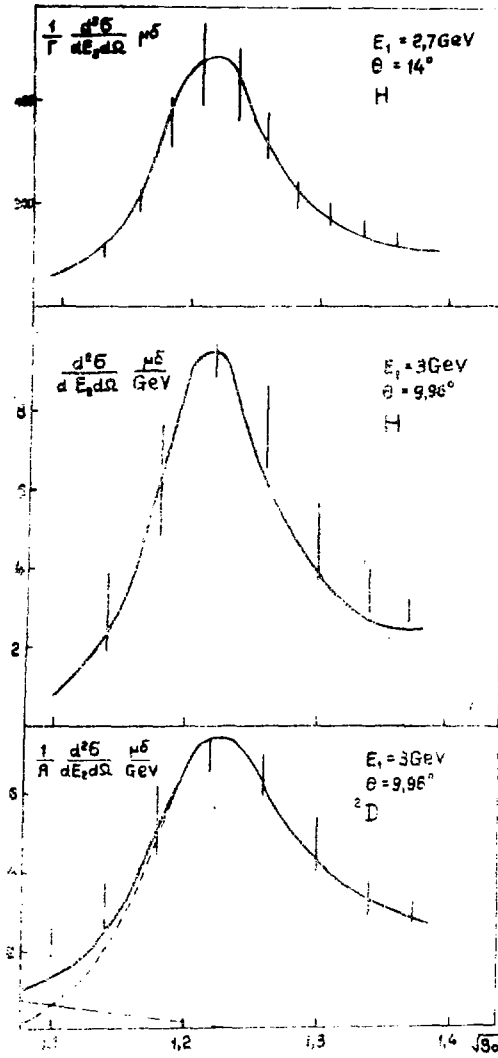


Fig. 2

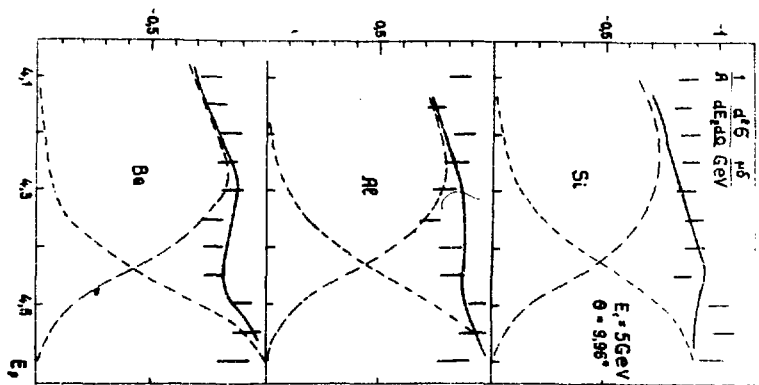


FIG. 5

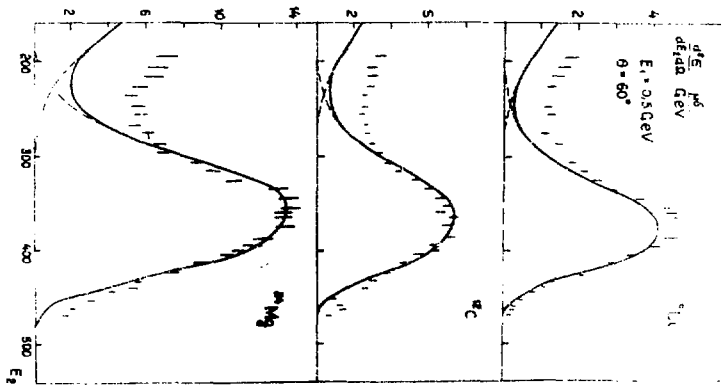


FIG. 4

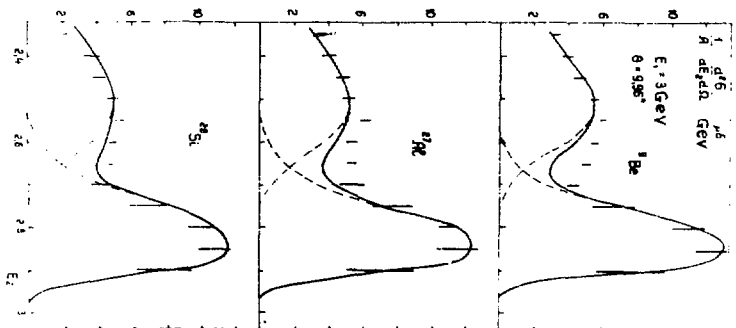


FIG. 3

Figure Captions

- Fig.1. The impulse approximation diagram.
- Fig.2. The cross section of (e, e') process versus the invariant mass $\sqrt{W} = \sqrt{S}$ for scattering on protons - experiment [10] at $\lambda^2 = 0.35 \text{ (GeV/c)}^2$, $E_1 = 2.7 \text{ GeV}$; on protons and neutrons - experiment [2] at $\lambda^2 \approx 0.23 \text{ (GeV/c)}^2$, $E_1 = 3 \text{ GeV}$.
- Fig.3. Scattered electron energy spectra for Be, Al, Si target nuclei - experiment [2] at $\lambda^2 \sim 0.25 \text{ (GeV/c)}^2$.
- Fig.4. Scattered electron energy spectra for Li, C, Mo target nuclei - experiment [1] at $\lambda^2 \sim 0.19 \text{ (GeV/c)}^2$.
- Fig.5. Scattered electron energy spectra for Ge, Si, S target nuclei - experiment [2] at $\lambda^2 \sim 0.66 \text{ (GeV/c)}^2$.

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Δ - ИЗОБАРЫ И КВАЗИПРУТОГО ПИКА

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